

# GLOBAL POSITIONING SYSTEM (GPS) PERFORMANCE

QUARTERLY REPORT 4 (OCTOBER TO DECEMBER  
2021)

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## TABLE OF CONTENTS

1. INTRODUCTION .....	5
1.1. PURPOSE .....	5
1.2. DOCUMENT OVERVIEW .....	5
1.3. REFERENCES .....	5
1.3.1. Applicable Documents .....	5
1.3.2. Reference Documents.....	6
1.4. ACRONYMS .....	6
2. INTRODUCTION .....	7
2.1. PURPOSE .....	7
2.2. PERFORMANCE SPECIFICATION AND DEFINITIONS .....	7
2.3. METHODOLOGY .....	10
2.4. ASSUMPTIONS.....	13
3. SPS PERFORMANCE .....	14
3.1. BASELINE 24-SLOT CONSTELLATION.....	14
3.2. SPS SIS ACCURACY .....	14
3.3. SPS SIS INTEGRITY.....	17
3.4. SPS SIS CONTINUITY .....	17
3.5. SPS SIS AVAILABILITY.....	17
3.6. PDOP AVAILABILITY .....	18
3.7. POSITION SERVICE AVAILABILITY.....	19
3.8. POSITIONING ACCURACY .....	20
4. NANU ANALYSIS .....	23
5. CONCLUSIONS.....	25
6. APPENDIX A: GEOMAGNETIC DATA .....	27

## LIST OF TABLES AND FIGURES

Table 1-1 Applicable Documents .....	5
Table 1-2 Reference Documents .....	6
Table 1-3 Acronyms .....	6
Table 2-1: SPS Criteria and Specifications.....	9
Table 3-1: Baseline constellation in the Period 1 October to 31 December 2021.....	14
Table 3-2: Range Error Statistics for Reporting Period .....	16
Table 4-1: Summary of Forecast Scheduled Outages.....	23
Table 4-2: Summary of Actual Scheduled Outages .....	23
Table 4-3: Summary of Cancelled Outages .....	23
Table 4-4: Summary of Forecast and Actual Unscheduled Outages.....	23
Table 4-5: Summary of NANU Statistics for Monitoring Period .....	24
Table 5-1: Summary of Performance.....	25
Figure 2-1: Location of EUREF Sites ( <a href="http://www.epncb.oma.be/_networkdata/stationmaps.php">http://www.epncb.oma.be/_networkdata/stationmaps.php</a> ).....	11
Figure 3-1: Constellation URE (95%) for Reporting Period.....	15
Figure 3-2: Constellation RMS URE for Reporting Period .....	15
Figure 3-3: Daily PDOP Availability in the Reporting Period .....	18
Figure 3-4: Daily Maximum PDOP Value in the Reporting Period .....	19
Figure 3-5: Daily Horizontal Service Availability Values for Reporting Period.....	20
Figure 3-6: Daily Vertical Service Availability Values for Reporting Period .....	20
Figure 3-7: Daily Horizontal Position Accuracy (95%) for Reporting Period .....	21
Figure 3-8: Daily Vertical Position Accuracy (95%) for Reporting Period.....	21
Figure 3-9: Daily Horizontal Position Accuracy (99.99%) for Reporting Period .....	22
Figure 3-10: Daily Vertical Position Accuracy (99.99%) for Reporting Period .....	22
Figure 6-1: K-Index Values at Lerwick during Reporting Period.....	27
Figure 6-2: K-Index Values at Eskdalemuir during Reporting Period .....	28
Figure 6-3: K-Index Values at Hartland during Reporting Period .....	28

## 1. INTRODUCTION

### 1.1. PURPOSE

This document presents the results of the GPS SPS performance assessment for the period of October to December 2021. The objectives of the study are to compare the measured performance against US DoD SPS performance specification [RD.1], covering the following parameters [AD.1]:

- SPS SiS Accuracy,
- SPS SiS Integrity,
- SPS SiS Continuity,
- SPS SiS Availability,
- PDOP Availability,
- SPS Position Service Availability and
- SPS Position Service Accuracy.

It also includes NANU analysis and geomagnetic activity. The performance is analysed using raw data recorded at the EUREF site SHOE, in the South of the UK.

### 1.2. DOCUMENT OVERVIEW

This document is arranged in the following sections:

- **Section 1**, the current section, describes the purpose, scope and structure of the document and lists the reference documents.
- **Section 2** gives an introduction to the activity, including performance specification and assessment methodology and assumptions;
- **Section 3** contains an assessment of performance against GPS SPS performance standards;
- **Section 4** provides an analysis of the NANUs;
- **Section 5** contains the conclusions;
- **Section 6** (Appendix A) provides the geomagnetic activity data.

### 1.3. REFERENCES

#### 1.3.1. APPLICABLE DOCUMENTS

The following documents, of the exact issue shown, form part of this document to the extent specified herein. Applicable documents are those referenced in the Contract or approved by the Approval Authority. They are referenced in this document in the form [AD.x]:

**Table 1-1 Applicable Documents**

Ref.	Title	Code	Version	Date
[AD.1]	THE PROVISION OF MONITORING AND ANALYSIS OF GPS SIGNALS IN SPACE –	CONTRACT NO. 1762 (AMENDMENT NO. 9)	-	08/12/20
[AD.2]				
[AD.3]				
[AD.4]				

### 1.3.2. REFERENCE DOCUMENTS

The following documents, although not part of this document, amplify or clarify its contents. Reference documents are those not applicable and referenced within this document. They are referenced in this document in the form [RD.x]:

**Table 1-2 Reference Documents**

Ref.	Title	Code	Version	Date
[RD.1]	Global Positioning System Standard Positioning Service Performance Standard	GPS SPS	5 <sup>th</sup> Edition	Apr 2020
[RD.2]	Global Positioning System (GPS) Civil Monitoring Performance Specification	DOT-VNTSC-FAA-09-08	-	April 30 <sup>th</sup> 2009
[RD.3]	Reference Set of Parameters for RAIM Availability Simulations', EUROCAE WG-62	-	-	8-9 July 2003
[RD.4]	The International GNSS Service in a changing landscape of Global Navigation Satellite Systems	Journal of Geodesy 83: 191-198		2009

### 1.4. ACRONYMS

Acronyms used in this document and needing a definition are included in the following table:

**Table 1-3 Acronyms**

Acronym	Definition
AOD	Age Of Data
CAA	Civil Aviation Authority
GNSS	Global Navigation Satellite System
GPS	Global Positioning System
HDOP	Horizontal Dilution Of Precision
IGS	International GNSS Service
NANU	Notice Advisory to Navstar Users
NOTAM	Notice To Airmen
PDOP	Position Dilution Of Precision
RAIM	Receiver Autonomous Integrity Monitoring
SIS	Signal In Space
SPS	Standard Positioning Service
TTA	Time To Alarm
UERE	User Equivalent Range Error
URA	User Range Accuracy
URE	User Range Error
VDOP	Vertical Dilution Of Precision

## 2. INTRODUCTION

### 2.1. PURPOSE

The purpose of the performance monitoring activity is to collect and analyse data on the performance of the GPS Signal in Space (SIS) [AD.1]. For this report, the applicable requirements are defined in the Global Positioning System Standard Positioning Service Performance Standard (GPS SPS PS), approved by the US Department of Defence [RD.1].

### 2.2. PERFORMANCE SPECIFICATION AND DEFINITIONS

The applicable performance specifications for the Standard Positioning Service [RD. 1] are as follows, with changes to the previous version of the GPS performance spec (prior to April 2020) noted:

Criteria	Specifications
SPS SIS Accuracy	<p><b>The User Range Error (URE) for any healthy satellite for Single-Frequency C/A-Code:</b></p> <ul style="list-style-type: none"> <li>• <math>\leq 7.0</math> m 95% Global Average URE during Normal Operations over all age of data (AODs) [<i>previous value was 7.8m</i>]</li> <li>• <math>\leq 3.8</math>m 95% Global Average URE during Normal Operations at Zero AOD [<i>previous value was 6.0m</i>]</li> <li>• <math>\leq 9.7</math> m 95% Global Average URE during Normal Operations at Any AOD [<i>previous value was 12.8m</i>]</li> <li>• <math>\leq 30</math> m 99.94% Global Average URE during Normal Operations over one-year period</li> <li>• <math>\leq 30</math> m 99.79% Worst Case Single Point Average URE during Normal Operations over one-year period</li> <li>• <math>\leq 388</math> m 95% Global Average URE during Extended Operations after 14 Days without Upload.</li> </ul> <p><b>The User Range Error (URE) for all healthy satellites for Single-Frequency C/A-Code:</b></p> <ul style="list-style-type: none"> <li>• <math>\leq 2.0</math> m 95% Global Average URE during Normal Operations over all age of data (AODs) [<i>New specification – did not appear previously</i>]</li> </ul> <p><b>The User Range Rate Error (URRE) for Single-Frequency C/A-Code:</b></p> <p><math>\leq 0.006</math> m/sec 95% Global Average URRE over any 3-second interval during Normal Operations at Any AOD</p> <p><b>The User Range Acceleration Error (URAE) for Single-Frequency C/A-Code:</b></p> <p><math>\leq 0.002</math> m/sec/sec 95% Global Average URAE over any 3-second interval during Normal Operations at Any AOD</p> <p><b>The UTC Offset Error for Single-Frequency C/A-Code:</b></p> <p><math>\leq 30</math> nsec 95% Global Average UTCOE during Normal Operations at Any AOD [<i>previous value was 40nsec</i>]</p>
SPS SIS Integrity	<p><b>The SIS Instantaneous URE Integrity for Single-Frequency C/A-Code:</b></p>

Criteria	Specifications
	<ul style="list-style-type: none"> <li>• <math>\leq 1 \times 10^{-5}</math> Probability Over Any Hour of the SPS SIS Instantaneous URE Exceeding the NTE Tolerance Without a Timely Alert during Normal Operations</li> </ul> <p><b>The SIS Instantaneous UTCOE Integrity for Single-Frequency C/A-Code:</b></p> <ul style="list-style-type: none"> <li>• <math>\leq 1 \times 10^{-5}</math> Probability Over Any Hour of the SPS SIS Instantaneous UTCOE Exceeding the NTE Tolerance Without a Timely Alert during Normal Operations</li> </ul> <p><b>The SIS Instantaneous Psat and Pconst for Single-Frequency C/A-Code:</b></p> <ul style="list-style-type: none"> <li>• <math>\leq 1 \times 10^{-5}</math> Fraction of Time when the SPS SIS Instantaneous URE Exceeds the NTE Tolerance Without a Timely Alert (Psat) <b>[New specification – did not appear previously]</b></li> <li>• <math>\leq 1 \times 10^{-8}</math> Fraction of Time when the SPS SIS Instantaneous URE from two or more satellites Exceeds the NTE Tolerance due to a common cause Without a Timely Alert (Pconst) <b>[New specification – did not appear previously]</b></li> </ul>
SPS SIS Continuity	<p><b>SPS SIS Unscheduled Failure Interruption Continuity</b></p> <ul style="list-style-type: none"> <li>• <math>\geq 0.9998</math> Probability Over Any Hour of Not Losing the SPS SIS Availability from a Slot Due to Unscheduled Interruption</li> <li>• Given that the SPS SIS is available from the slot at the start of the hour</li> </ul>
Status and Problem reporting	<p><b>Scheduled Event Affecting Service</b></p> <ul style="list-style-type: none"> <li>• Appropriate NANU issued to the Coast Guard and the FAA at least 48 hours prior to the event for 95% of the events <b>[previously did not specify a %]</b></li> </ul>
SPS SIS Availability	<p><b>SPS SIS Per-Slot Availability</b></p> <ul style="list-style-type: none"> <li>• <math>\geq 0.957</math> Probability that a Slot in the Baseline 24-Slot Configuration will be Occupied by a Satellite Broadcasting a Healthy SPS SIS</li> <li>• <math>\geq 0.957</math> Probability that a Slot in the Expanded Configuration will be Occupied by a Pair of Satellites Each Broadcasting a Healthy SPS SIS</li> </ul> <p><b>SPS SIS Constellation Availability</b></p> <ul style="list-style-type: none"> <li>• <math>\geq 0.98</math> Probability that at least 21 Slots out of the 24 Slots will be Occupied Either by a Satellite Broadcasting a Healthy SPS SIS in the Baseline 24-Slot Configuration or by a Pair of Satellites Each Broadcasting a Healthy SPS SIS in the Expanded Slot Configuration</li> <li>• <math>\geq 0.99999</math> Probability that at least 20 Slots out of the 24 Slots will be occupied either by a Satellite Broadcasting a Healthy SPS SIS in the Baseline 24-Slot Configuration or by a Pair of Satellites Each Broadcasting a Healthy SPS SIS in the Expanded Slot Configuration.</li> <li>• <math>\geq 0.95</math> Probability that the Constellation will have at least 24 Operational Satellites regardless of Whether Those Operational Satellites are Located in Slots or Not.</li> </ul>
PDOP Availability	<ul style="list-style-type: none"> <li>• <math>\geq 98\%</math> global Position Dilution of Precision (PDOP) of 6 or less</li> <li>• <math>\geq 88\%</math> worst site PDOP of 6 or less</li> </ul>
SPS Position Service Availability	<ul style="list-style-type: none"> <li>• <math>\geq 99\%</math> Horizontal Service Availability average location</li> <li>• <math>\geq 90\%</math> Horizontal Service Availability worst-case location</li> </ul>



Criteria	Specifications
	<ul style="list-style-type: none"> <li>• <math>\geq 99\%</math> Vertical Service Availability average location</li> <li>• <math>\geq 90\%</math> Vertical Service Availability worst-case location</li> </ul> <p><b>With 15 m horizontal and 33 m vertical (SIS only) 95% threshold over 24hours</b>  <i><b>[previous values were 17m and 37m]</b></i></p>
Positioning Accuracy	<ul style="list-style-type: none"> <li>• <math>\leq 8</math> meters 95% Global Average Horizontal Error <i><b>[previous value was 9m]</b></i></li> <li>• <math>\leq 15</math> meters 95% worst site Horizontal Error <i><b>[previous value was 17m]</b></i></li> <li>• <math>\leq 13</math> meters 95% Global Average Vertical Error <i><b>[previous value was 15m]</b></i></li> <li>• <math>\leq 33</math> meters 95% worst site Vertical Error <i><b>[previous value was 37m]</b></i></li> <li>• Global Average Velocity Accuracy</li> <li>• <math>\leq 0.2</math> m/sec 95% velocity error, any axis <i><b>[New specification – did not appear previously]</b></i></li> <li>• <math>\leq 30</math> nanoseconds time transfer error 95% of time for Time Transfer Domain Accuracy <i><b>[previous value was 40nsec]</b></i></li> </ul>

**Table 2-1: SPS Criteria and Specifications**

The definitions for each of the criteria and the methodology used for assessment are given below. As well as the GPS SPS [RD.1], the GPS civil monitoring performance specification [RD.2] has also been used to help define the methodology for the assessment.

### SPS SIS Accuracy

The SPS SIS accuracy is described in two statistical ways; one way is as the 95th percentile (95%) SPS SIS user range error (URE) at a specified age of data (AOD), the other is as the 95% SPS SIS URE over all AODs. With either statistical expression, the SPS SIS accuracy is also known as the SPS SIS pseudorange accuracy. In this context, “pseudorange” means the full pseudorange data set (i.e., the matched combination of a corrected pseudorange measurement and a pseudorange origin, or equivalently the matched combination of a raw pseudorange measurement and the associated NAV data).

Other accuracy-related SPS SIS performance parameters include the SPS SIS pseudorange rate (velocity) accuracy defined as the 95% SPS SIS pseudorange rate error over all AODs and the SPS SIS pseudorange acceleration (rate rate) accuracy defined as the 95% SPS SIS pseudorange acceleration error over all AODs. These values are not monitored as part of this performance monitoring contract.

### SPS SIS Integrity

The SPS SIS integrity is defined as the trust which can be placed in the correctness of the information provided by the SPS SIS. SPS SIS integrity includes the ability of the SPS SIS to provide timely alerts to receivers when the SPS SIS should not be used for positioning or timing. The SPS SIS should not be used when it is providing misleading signal-in-space information (MSI), where the threshold for “misleading” is a not-to-exceed (NTE) tolerance on the SIS URE. For this SPS PS, the four components of integrity are the probability of a major service failure, the time to alert, the SIS URE NTE tolerance, and the alert (either one or the other of two types of alerts).

- Probability of a Major Service Failure. The probability of a major service failure for the SPS SIS is defined to be the probability that the SPS SIS instantaneous URE exceeds the SIS URE NTE tolerance (i.e., MSI) without a timely alert being issued (i.e., unalerted MSI [UMSI]). Alerts generically include both alarms and warnings.

- Time to Alert. The time to alert (TTA) for the SPS SIS is defined to be the time from the onset of MSI until an alert (alarm or warning) indication arrives at the receiver's antenna. Real-time alert information broadcast as part of the NAV message data is defined to arrive at the receiver's antenna at the end of the NAV message subframe which contains that particular piece of real-time alert information.
- SIS URE NTE Tolerance. The SPS SIS URE NTE tolerance for a healthy SPS SIS is defined to be 4.42 times the upper bound on the URA value corresponding to the URA index "N" currently broadcast by the satellite. The SIS URE NTE tolerance for a marginal SPS SIS is not defined and there is no SIS URE NTE tolerance for an unhealthy SPS SIS.

### **SPS SIS Continuity**

The SPS SIS continuity for a healthy SPS SIS is the probability that the SPS SIS will continue to be healthy without unscheduled interruption over a specified time interval. Scheduled interruptions which are announced at least 48 hours in advance do not contribute to a loss of continuity. Scheduled SPS SIS interruptions are announced by way of the Control Segment issuing a "Notice Advisory to Navstar Users" (NANU). NANUs are similar to the "Notices to Airmen" (NOTAMs) issued regarding scheduled interruptions of ground-based air navigation aids. OCS internal procedures are to issue NANUs for scheduled interruptions at least 96 hours in advance.

### **SPS SIS Availability**

The SPS SIS availability is the probability that the slots in the GPS constellation will be occupied by satellites transmitting a trackable and healthy SPS SIS. For this SPS Performance Standard, there are two components of availability as follows:

- Per-Slot Availability. The fraction of time that a slot in the GPS constellation will be occupied by a satellite that is transmitting a trackable and healthy SPS SIS.
- Constellation Availability. The fraction of time that a specified number of slots in the GPS constellation

### **PDOP Availability**

PDOP availability is defined as the percentage of time over a specified time interval that the predicted PDOP is less than a specified value for any point within the service volume [RD.1].

### **Position Service Availability**

Position service availability is defined as the percentage of time over a specified time interval that the position accuracy is less than a specified value for any point within the service volume [RD.1].

### **Positioning Service Accuracy**

Position service accuracy is defined as the statistical difference between position measurements and a surveyed benchmark for any point within the service volume over a specified time interval [RD.1].

## **2.3. METHODOLOGY**

For the performance analysis in this report, raw GPS measurement data from reference stations has been analysed. The primary source of data is the EUREF permanent GPS network (as shown in the next figure).



**Figure 2-1: Location of EUREF Sites**  
 (<http://www.epncb.oma.be/networkdata/stationmaps.php>)

The EUREF receivers provide high rate (1Hz), multi-constellation, multi-frequency GNSS measurements. The data files are accessed via ftp and can be downloaded at GMV NSL before processing with GISMO SW. The daily navigation message files are also downloaded from the IGS ftp site and used to provide the navigation data [RD.4].

As only a single site is required for the performance monitoring, SHOE<sup>1</sup> has been chosen. Therefore during this monitoring period the SHOE site is used as the main source of 1Hz data, and hence the performance statistics during this period are mainly based on data from that site. The only exception is 6<sup>th</sup> October where there was a big gap and so data from the OS SHRE site (Shrewsbury) has been used instead on that day.

The methods for assessing of each of the requirements are described below.

### SPS SIS Accuracy

SIS accuracy is assessed through processing and analysis of the raw measurement data. In order to compute the SIS accuracy, the measurements recorded at the GPS receiver are used to compute the instantaneous SIS errors. This is done by computing the difference between computed ranges (based on known receiver location and satellite position) and the corrected measurement, which has satellite and receiver clock biases, group delay, ionospheric and tropospheric errors removed. Once the SIS range errors for every satellite measurement on every epoch have been computed, the per-satellite and all satellite statistics across the whole period, as well as daily statistics for all satellites combined, are generated.

### SPS SIS Integrity

SIS accuracy is assessed through processing and analysis of the raw measurement data. The SIS integrity is assessed by comparing each instantaneous computed SIS error value with a threshold value of  $4.42 \times \text{broadcast URA}$ . The number of occasions where the instantaneous URE exceeds the threshold are counted and checked against the expected number of failures.

### SPS SIS Continuity

<sup>1</sup> Note that usually DARE is chosen but the data for DARE was unavailable after mid-November for some reason and so SHOE has been chosen instead.

SIS continuity is assessed through analysis of the broadcast navigation messages and the NANU archive. Firstly, the daily broadcast navigation messages are scanned in order to find the time periods for any satellites that do not have healthy navigation messages. These satellites and time periods are then matched against NANU information to see if the outages are scheduled or unscheduled.

The SIS continuity is computed for the baseline 24-slot constellation and is an average value over all slots. The total time that any satellites in the baseline constellation were unhealthy due to an unscheduled outage is divided by the total time in the analysis period and expressed as a percentage. Results are presented for the reporting period and, when available, for the previous year.

### **SPS SIS Availability**

SIS availability is assessed through analysis of the broadcast navigation messages and the NANU archive. Firstly, the daily broadcast navigation messages are scanned in order to find the time periods for any satellites that do not have healthy navigation messages. These satellites and time periods are then matched against NANU information to see if the outages are scheduled or unscheduled.

The SIS availability is computed for the baseline 24-slot constellation as well as for the whole constellation and is an average value over all slots. At each epoch the number of healthy satellites (both in the baseline 24-slot constellation and in total) is counted. Then the following parameters are computed:

- Total time that there are less than 21 healthy satellites in the baseline constellation;
- Total time that there are less than 20 healthy satellites in the baseline constellation;
- Total time that there are less than 24 healthy satellites in the whole constellation.

These parameters are then divided by total time of the analysis and expressed as percentage values. Results are presented for the reporting period and, when available, for the previous year.

It should be noted that in case the baseline 24-slot constellation does not meet requirements, the analysis will be expanded to include pairs of satellites in the expanded slot constellation.

### **PDOP Availability**

PDOP availability is assessed through processing and analysis of the raw measurement data. The PDOP availability is assessed by computing the PDOP for all satellites in view above 5 degrees at the GPS receiver at every epoch (1Hz rate). Each PDOP value is checked against the threshold value of 6 and any failures are counted. The numbers of failures on each day are then used to generate the daily availability value. A separate availability value for each day is computed.

### **Position Service Availability**

Position service availability is assessed through processing and analysis of the raw measurement data. The derivation of the position service availability requirements of 15m (95% horizontal accuracy) and 33m (95% vertical accuracy) for 99% of the time are explained a bit more in section B.3.2 of the GPS SPS [RD.1]. The requirement is based on fulfilling a 1-sigma UERE of 3.6m, HDOP of 2.1 and VDOP of 4.53. To check this requirement, the following approach is used:

- For each day, compute daily rms SIS error for all satellites combined. This is equivalent to the 1-sigma UERE in the description above;
- On each epoch, multiply daily rms SIS error by HDOP value to compute estimated horizontal accuracy due to SIS error;
- For each epoch, multiply daily rms SIS error by VDOP value to compute estimated vertical accuracy due to SIS error;
- Compute daily availability (%) of estimated horizontal accuracy < 7.5m (1-sigma);
- Compute daily availability (%) of estimated vertical accuracy < 16.5m (1-sigma).
- If daily availability of horizontal accuracy greater than the required threshold, the requirement for horizontal service accuracy is passed;

- If daily availability of vertical accuracy greater than the required threshold, the requirement for vertical service accuracy is passed.

### Positioning Service Accuracy

In order to check the position service accuracy, the raw measurements recorded at the GPS receiver are used to compute a user position solution on every epoch (1Hz). The computed positions are then compared against the known position of the receiver in order to generate horizontal and vertical position errors. Statistics for 95% error value, 99.99% error value etc. are then computed separately for each day and checked against the thresholds.

## 2.4. ASSUMPTIONS

For processing the raw data and generating the results the following assumptions are made:

- Single frequency (L1) processing with C/A code;
- 5-degree elevation mask used;
- Broadcast iono model (Klobuchar) used to remove ionospheric errors;
- RTCA trop model used to remove tropospheric errors;
- Weighted least squares RAIM algorithm used for RAIM prediction (protection level computation) and Fault Detection;
- Probability of missed detection = 0.001 and Probability of false alarm =  $1 \times 10^{-5}$  for RAIM computations;
- UERE budget (non-SIS components) used in position solution and for RAIM predictions based given below [RD.3]:

Elevation, degrees	Error, metres
5	7.48
10	6.64
15	5.92
20	5.31
30	4.31
40	3.57
50	3.06
60	2.73
90	2.44

- The URA value from the broadcast navigation message is combined with the values in the table to form the total UERE for the observations.

As the actual monitoring is based on the measurements from one receiver, the following points should be noted:

- Performance monitoring is local to the monitoring station with a coverage area defined by the correlation of the major error sources and the configuration of the constellation.
- The range domain errors contain the residuals of other error sources other than the SIS range errors, hence the performance statistics generated are conservative.

### 3. SPS PERFORMANCE

#### 3.1. BASELINE 24-SLOT CONSTELLATION

The SPS SIS performance standard is largely based on the GPS baseline 24-slot constellation, which consists of 24 slots in six orbital planes with four slots per plane. Some of these slots are expanded, whereby two satellites occupy fore and aft positions at that slot, in which case the slot is occupied as long as at least one of the expanded slots is occupied by an operational satellite. It is important to identify the baseline constellation (and expanded slots) to act as reference to subsequent data processing and analysis. The following tables show the satellite PRN in each slot for the baseline constellation for the period October to December 2021<sup>2</sup>.

**Table 3-1: Baseline constellation in the Period 1 October to 31 December 2021**

Slot	A1	A2	A3	A4	B1A/B1F	B2	B3	B4	C1	C2	C3	C4A/C4F
PRN	24	31	30	7	16/26	25	14	12	29	27	8	19/17
Slot	D1	D2A/D2F	D3	D4	E1	E2	E3A/E3F	E4	F1	F2A/F2F	F3	F4
PRN	2	1/21	18	6	3	10	5/20	23	32	15/13	9	4

Note that in the latest version of the GPS SPS performance spec [RD.1] there are additional expandable slots defined for A2 but these are not currently used.

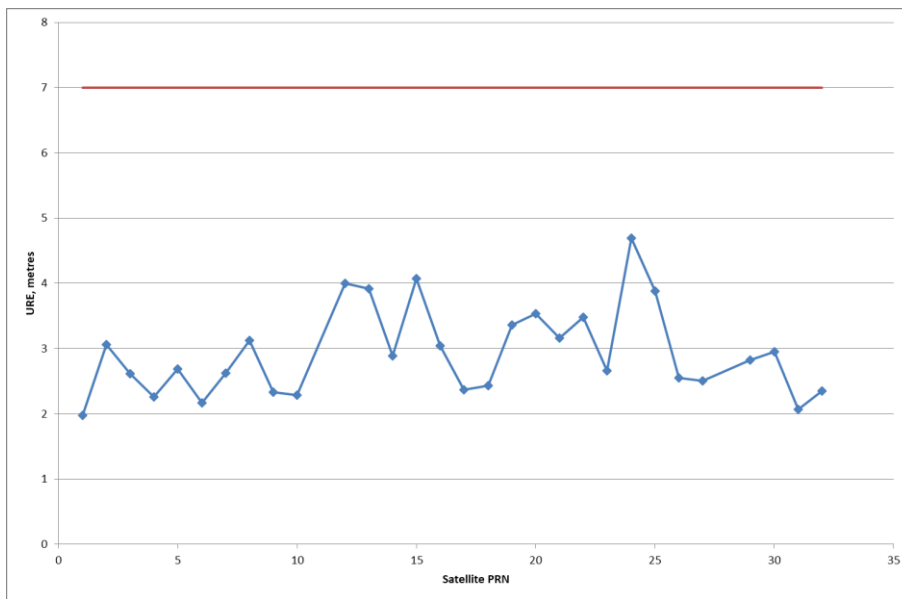
#### 3.2. SPS SIS ACCURACY

In addition to the specifications in Table 2-1, the Conditions and Constraints for SPS SIS URE Accuracy specification [RD.1] are:

- For any healthy SPS SIS
- Neglecting single-frequency ionospheric delay model errors
- Including group delay time correction (TGD) errors at L1
- Including inter-signal bias (P(Y)-code to C/A-code) errors at L1

The statistics presented here are based on the same sample rate for positioning (1Hz). It should be noted that the computed range errors (in addition to SIS errors) contain residual errors local to the monitoring antenna (multipath, tropospheric and ionospheric). The URE Accuracy (95th percentile) values of each satellite for the period October to December 2021 are shown in the next figure.

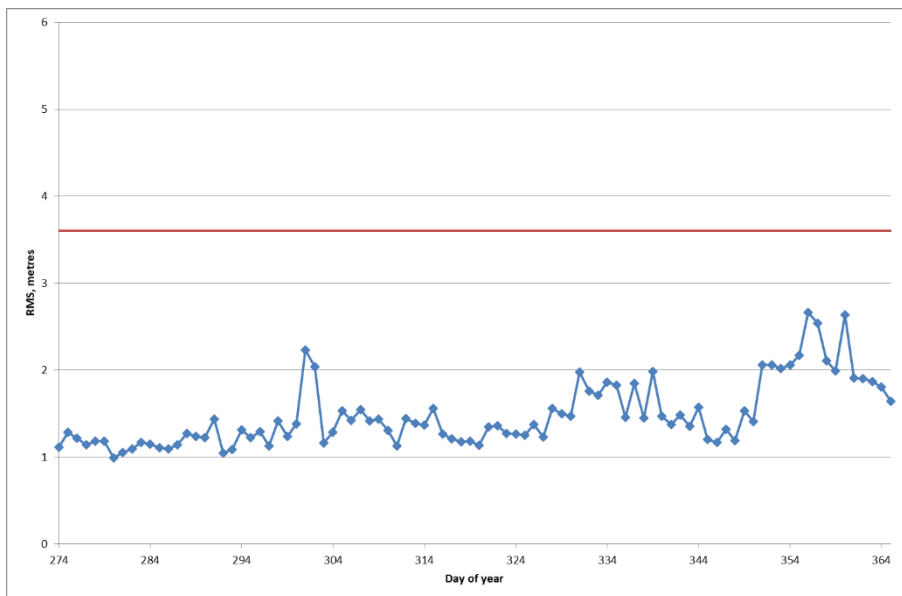
<sup>2</sup> The information on slots is taken from the figure at <https://www.navcen.uscg.gov/pdf/gps/current.pdf>. It is noted that there is some inconsistency between this figure and the slot numbers in the ops advisory messages. The figure was last updated on 1<sup>st</sup> Sep.



**Figure 3-1: Constellation URE (95%) for Reporting Period**

It can be seen that the URE (95%) for all satellites is below the 7m threshold.

The daily constellation RMS URE results in the period October to December 2021 and the 3.6m threshold are shown in the next figure. Note that  $\leq 7\text{ m}$  95% SPS SIS URE performance standard is equivalent to a  $\leq 3.6\text{ m}$  RMS SPS SIS URE performance standard [RD.1]. This is also important for the position service availability assessment.



**Figure 3-2: Constellation RMS URE for Reporting Period**

It can be seen that the RMS values are below the threshold (3.6 metres) on all days.

As well as the 95% and rms URE statistics, additional URE statistics are computed, including mean, 1-sigma and maximum values. Although not strictly required for the performance specification, these values can be useful for anomaly investigation. The range error statistics (in metres) for the period October to December 2021 are given in the table below.

**Table 3-2: Range Error Statistics for Reporting Period**

PRN	Range Error (mean)	Range Error (RMS)	1-sigma	Range Error (95%)	Range Error (max)	Number of Samples
1	0.31	1.04	0.99	1.98	9.91	2197991
2	1.13	1.61	1.15	3.06	6.96	2955043
3	0.52	1.47	1.38	2.61	8.53	1866709
4	0.32	1.13	1.08	2.26	6.87	2676162
5	0.58	1.29	1.15	2.69	7.57	2763215
6	0.06	1.08	1.08	2.17	12.99	2804703
7	0.40	1.30	1.24	2.63	7.88	2805968
8	0.88	1.69	1.44	3.12	8.73	2528578
9	0.61	1.24	1.08	2.33	8.24	2382599
10	0.82	1.20	0.87	2.29	10.05	2877337
12	1.03	1.77	1.44	4.00	8.15	2326358
13	1.25	1.91	1.44	3.92	7.76	2139111
14	0.52	1.35	1.24	2.88	9.55	2856369
15	0.91	1.87	1.63	4.07	26.67	2469589
16	1.18	1.71	1.24	3.05	23.94	2646392
17	0.25	1.18	1.15	2.37	23.84	2923280
18	0.99	1.36	0.93	2.44	6.03	2787587
19	1.26	1.72	1.17	3.36	7.60	2862443
20	1.18	1.77	1.32	3.54	8.07	2676772
21	1.86	2.06	0.88	3.16	9.88	2256841
22	1.67	2.01	1.12	3.48	6.70	1469171
23	0.89	1.35	1.02	2.66	11.59	2900032
24	1.56	2.18	1.52	4.69	8.17	2143632
25	1.45	1.88	1.19	3.88	7.76	2169210
26	0.83	1.40	1.13	2.55	16.95	2503061
27	1.22	1.48	0.85	2.51	8.28	1941128
29	1.08	1.54	1.09	2.82	6.63	2632990
30	0.53	1.51	1.41	2.95	7.03	2607994
31	0.32	1.11	1.06	2.07	4.81	2787507
32	0.79	1.27	0.99	2.35	8.58	2876059
Total	0.74	1.36	1.14	2.93	26.67	75833831

Overall, the measured SIS accuracy for any satellite is below the threshold values throughout the monitoring period for each satellite.

The measured accuracy for all satellites combined is above the threshold of 2m, although it should be noted that the specification does not include ionospheric errors whereas as the measurements used in the analysis will include residual iono errors and hence will be larger.



### 3.3. SPS SIS INTEGRITY

In addition to the specifications in Table 2-1, the Conditions and Constraints for SPS SIS Integrity performance [RD.1] are:

- For any healthy SPS SIS;
- SPS SIS URE NTE tolerance defined to be  $\pm 4.42$  times the upper bound on the URA value corresponding to the URA index "N" currently broadcast by the satellite;
- Given that the maximum SPS SIS instantaneous URE did not exceed the NTE tolerance at the start of the hour;
- Worst case for delayed alert is 6 hours;
- Neglecting single-frequency ionospheric delay model errors.

Based on the requirement of  $1 \times 10^{-5}$ /hr probability for misleading information, 91-day period and a 31-satellite constellation, the maximum number of events expected is 0.66.

On every epoch throughout the monitoring period, the instantaneous measured URE for each satellite has been compared against a threshold of 4.42 times the upper value of the URA index. The number of URE values above the threshold has been recorded and is checked against the expected number.

From the analysis there are 0 days where this condition is met – therefore the SIS integrity requirement is passed in this period.

### 3.4. SPS SIS CONTINUITY

In addition to the specifications in Table 2-1, the Conditions and Constraints for SPS SIS Continuity performance [RD.1] are:

- Calculated as an average over all slots in the 24-slot constellation, normalized annually;
- Given that the SPS SIS is available from the slot at the start of the hour.

During this reporting period there was one unscheduled event but it was not on the baseline constellation. Therefore this gives a continuity figure of 100% in this period, which meets the requirement of 99.98% in this period.

For the previous rolling year, there have been 2 unscheduled outage on the baseline constellation lasting for 5.37 hrs in total. This gives a continuity value for the year of 99.997%, which meets the performance standard.

### 3.5. SPS SIS AVAILABILITY

In addition to the specifications in Table 2-1, the Conditions and Constraints for SPS SIS Availability performance [RD.1] are:

- Calculated as an average over all slots in the 24-slot constellation, normalized annually;
- Applies to satellites broadcasting a healthy SPS SIS which also satisfy the other performance standards in this SPS Performance Standard.

The total period (in this monitoring period) in which satellites from the baseline 24-satellite constellation broadcast an unhealthy SIS was 304.87 hours. This is equivalent to an average of 0.99425 over all slots in the 24-slot constellation and satisfies SPS SIS Per-slot Availability standard ( $\geq 0.957$ ).

The minimum number of the baseline constellation satellites broadcasting healthy SPS SIS was 23, greater than the specifications of 20 and 21. Hence, performance during the monitoring period was measured at the 100% level, satisfying the Performance Standard as specified below.

- $\geq 0.98$  Probability that at least 21 Slots out of the 24 Slots will be Occupied Either by a Satellite Broadcasting a Healthy SPS SIS in the Baseline 24-Slot Configuration or by a Pair of Satellites Each Broadcasting a Healthy SPS SIS in the Expanded Slot Configuration;
- $\geq 0.99999$  Probability that at least 20 Slots out of the 24 Slots will be occupied either by a Satellite Broadcasting a Healthy SPS SIS in the Baseline 24-Slot Configuration or by a Pair of Satellites Each Broadcasting a Healthy SPS SIS in the Expanded Slot Configuration.

The minimum number of operational satellites broadcasting healthy messages in this reporting period was 28. This represents performance at the 100% level, satisfying the Performance Standard as specified below.

- $\geq 0.95$  Probability that the Constellation has at least 24 operational satellites regardless of whether the operational satellites are located in the baseline slots.

For the previous rolling year, the total period in which satellites from the baseline 24-satellite constellation did not broadcast a healthy SIS was 629 hours. This is equivalent to an average of 0.99698 over all slots in the 24-slot constellation and satisfies SPS SIS Per-slot Availability ( $\geq 0.957$ ).

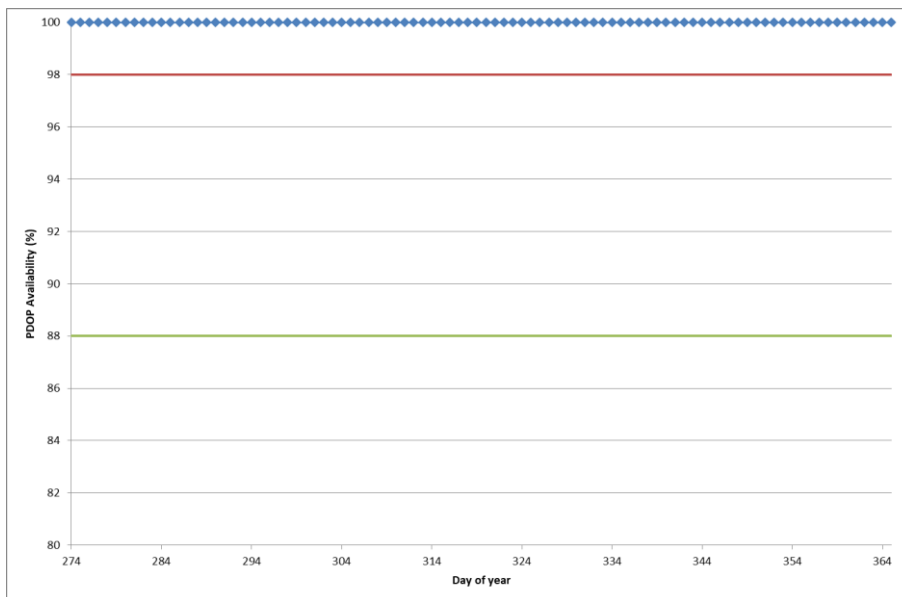
The minimum number of the baseline constellation satellites broadcasting healthy SPS SIS was 22, greater than the specifications of 20 and 21, and the minimum number of operational satellites broadcasting healthy messages was 28. This means that all constellation availability requirements from the Performance Standard are met for the previous year.

### 3.6. PDOP AVAILABILITY

In addition to the specifications in Table 2-1, the Conditions and Constraints for PDOP performance [RD.1] are:

- Defined for position solution meeting the representative user conditions and operating within the service volume over any 24-hour interval;
- Based on using only satellites transmitting standard code and indicating "healthy" in the broadcast navigation message.

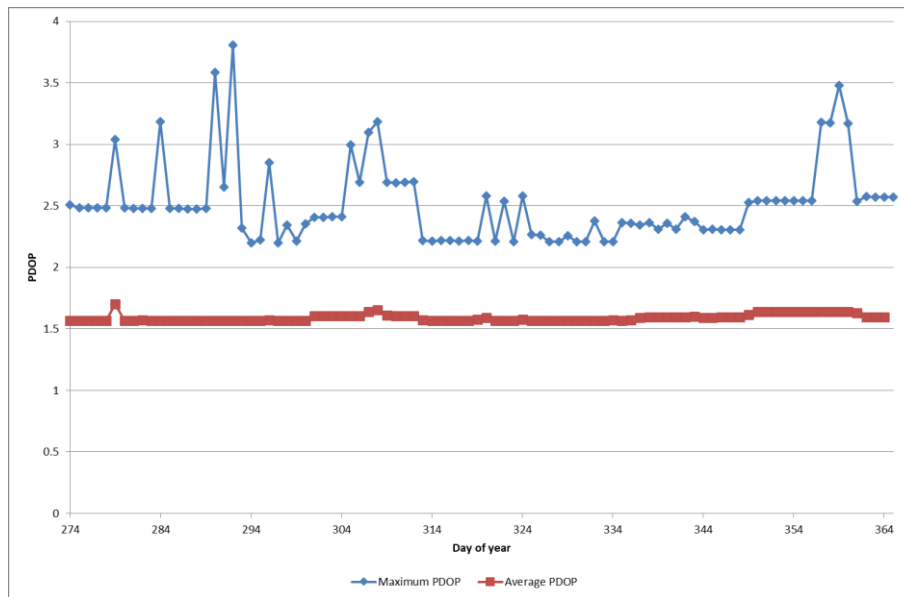
The following plot shows the daily PDOP availability (PDOP < 6) calculated at the site for all healthy satellites above 5 degrees elevation during the period October to December 2021.



**Figure 3-3: Daily PDOP Availability in the Reporting Period**

It can be seen that the daily PDOP availability values are all above the thresholds of 98% (global average) and 88% (worst site). Therefore, the PDOP availability fulfils the requirements.

In addition, the daily mean and maximum PDOP values are displayed for the same period.



**Figure 3-4: Daily Maximum PDOP Value in the Reporting Period**

The daily PDOP values PDOP can be used to identify specific days that have different performance from the others. It can be seen is that the maximum PDOP is well below the threshold of 6 on all days.

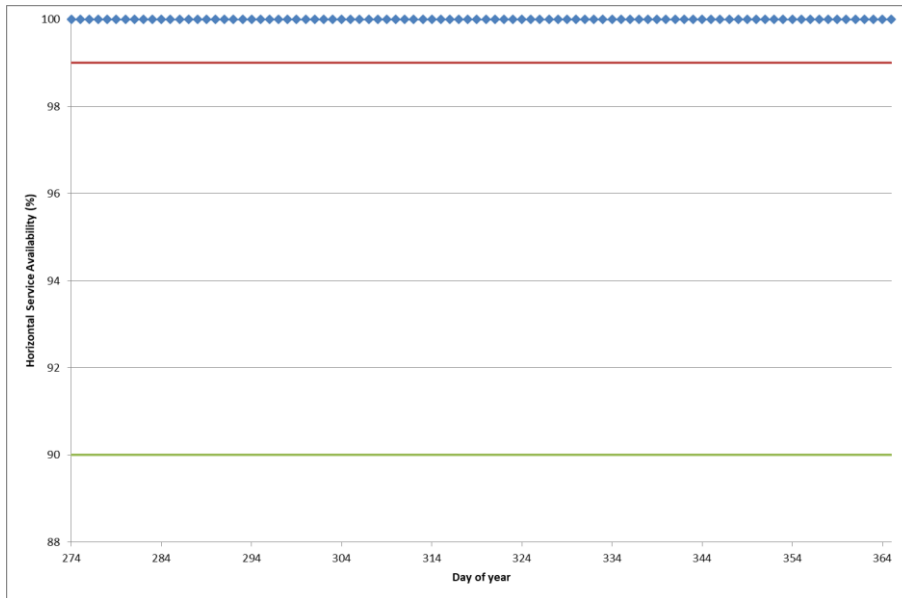
### 3.7. POSITION SERVICE AVAILABILITY

In addition to the specifications in Table 2-1, the Conditions and Constraints for Service Availability performance [RD.1] are:

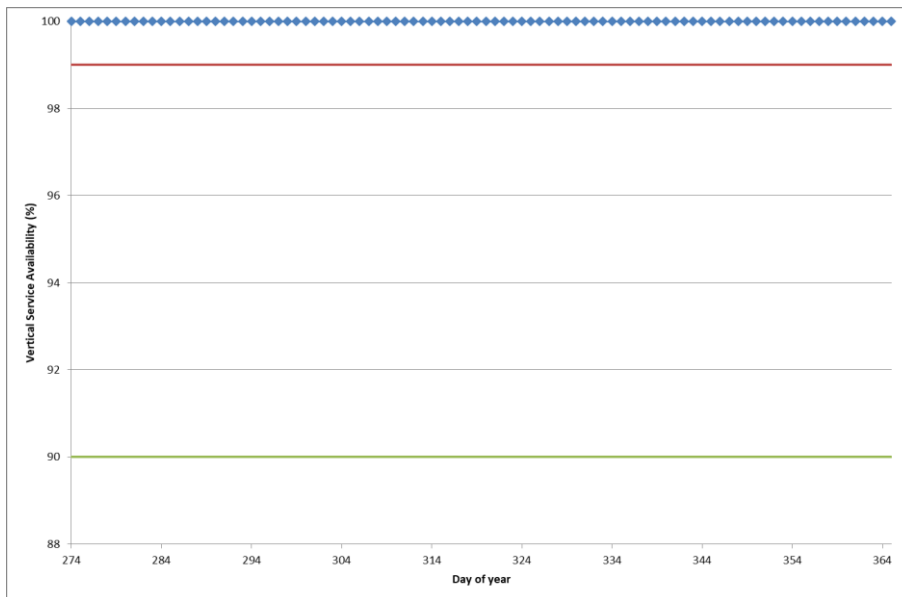
- 15 meters horizontal (SIS only) 95% threshold;
- 33 meters vertical (SIS only) 95% threshold;
- Defined for position solution meeting representative user conditions and operating within the service volume over any 24-hour interval;
- Based on using only satellites transmitting standard code and indicating “healthy” in the broadcast navigation message.

The computation of these values is detailed in section 2.3.

The daily horizontal and vertical service availabilities for the period October to December 2021 are shown in the following figures.



**Figure 3-5: Daily Horizontal Service Availability Values for Reporting Period**



**Figure 3-6: Daily Vertical Service Availability Values for Reporting Period**

These plots show the horizontal and vertical availability are well above the thresholds of 99% (global average) and 90% (worst site) for the reporting period. Therefore, the position service availability fulfils the requirements.

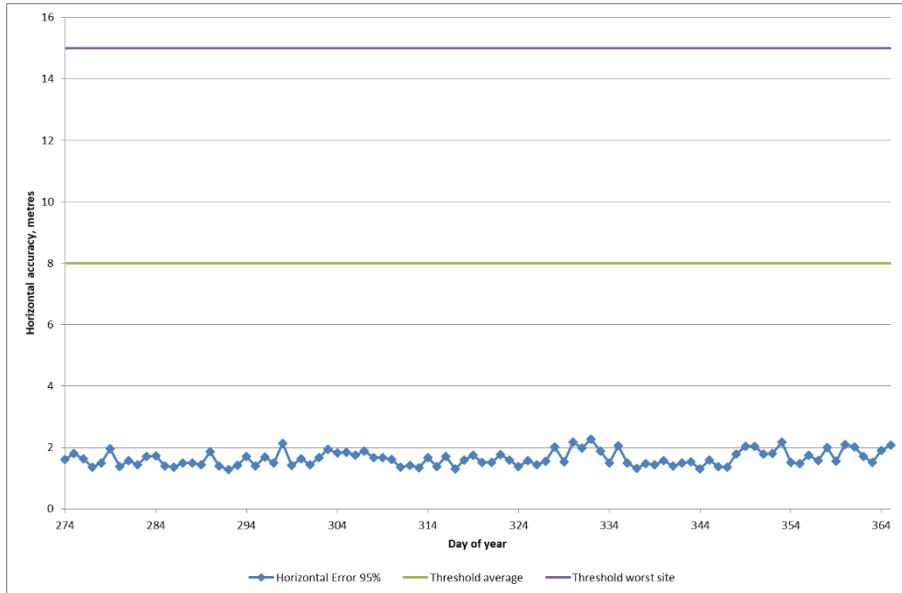
### 3.8. POSITIONING ACCURACY

In addition to the specifications in Table 2-1, the Conditions and Constraints for Positioning Accuracy performance [RD.1] are:

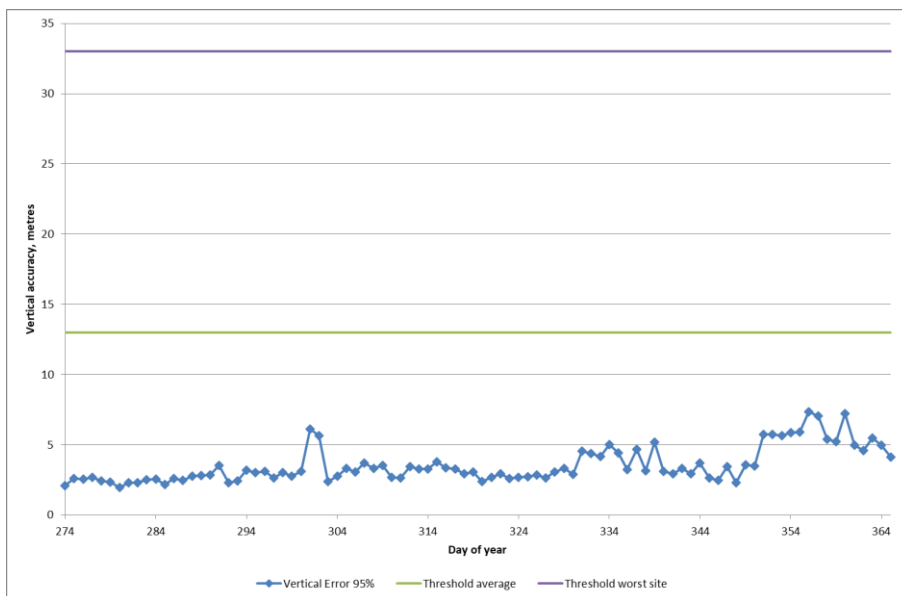
- Defined for position solution meeting the representative user conditions;
- Standard based on a measurement interval of 24 hours averaged over all points within the service volume.

For this monitoring activity it should be noted that the position accuracy is assessed through analysis of real data at a single point, rather than through service volume analysis.

The daily horizontal and vertical accuracy values (95%) for the period October to December 2021 are shown in the following figures.



**Figure 3-7: Daily Horizontal Position Accuracy (95%) for Reporting Period**

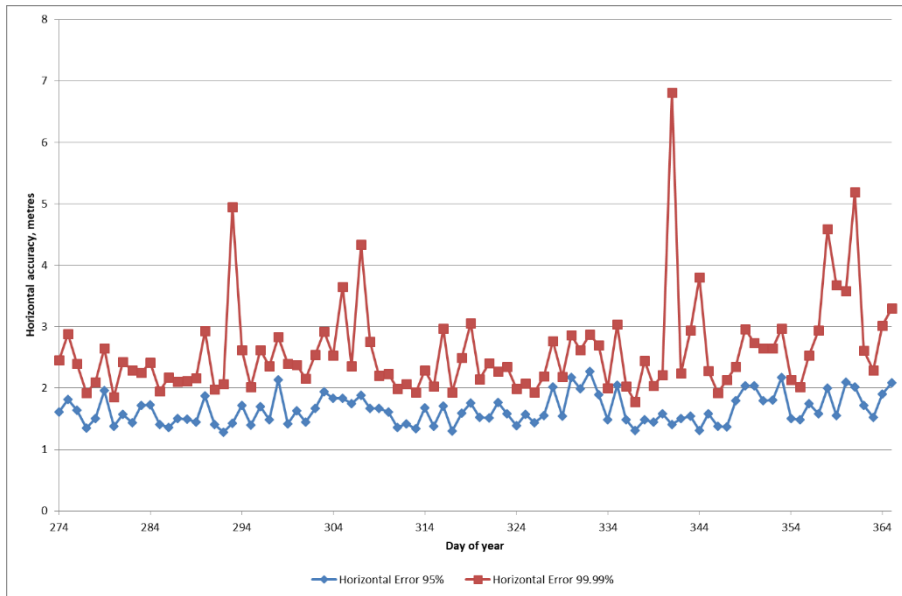


**Figure 3-8: Daily Vertical Position Accuracy (95%) for Reporting Period**

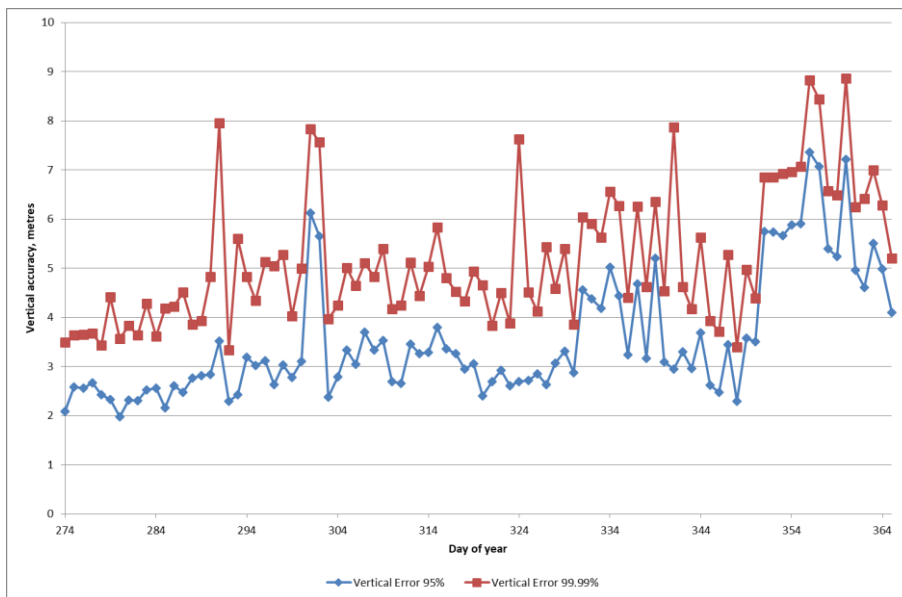
It can be seen that the daily horizontal accuracy values are all below the thresholds of 8m (global average) and 15m (worst site).

Also, the daily vertical accuracy values are well below the thresholds of 13m (global average) and 33m (worst site).

In addition, the daily position accuracy values at the 99.99% level are shown for the same period.



**Figure 3-9: Daily Horizontal Position Accuracy (99.99%) for Reporting Period**



**Figure 3-10: Daily Vertical Position Accuracy (99.99%) for Reporting Period**

It can be seen that on most days the 99.99% values generally follow the same pattern as the 95% values and are not significantly larger.

## 4. NANU ANALYSIS

(<http://www.navcen.uscg.gov/?pageName=gpsNanuInfo>). Summaries of the forecast and actual outages for scheduled and unscheduled events are given below. NANUs that affect the baseline constellation are highlighted in green. NANUs that affect one satellite of an expanded slot in the baseline constellation are highlighted in blue, tan or purple.

**Table 4-1: Summary of Forecast Scheduled Outages**

NANU	PRN	Type	Start day	Start Time	Stop day	Stop time	Outage (hours)	Ref
2021052	3	FCSTMX	300	1500	314	1500	336	E1
2021053	16	FCSTDV	319	2015	320	815	12	B1A
2021056	29	FCSTDV	337	300	337	1500	12	C1
2021057	2	FCSTDV	343	1245	344	45	12	D1
2021061	27	FCSTMX	349	1900	363	1900	336	D2F

**Table 4-2: Summary of Actual Scheduled Outages**

NANU	PRN	Type	Start day	Start Time	Stop day	Stop time	Outage (hours)	Ref
2021054	3	FCSTSUMM	300	1635	312	2124	292.8166	2021052
2021055	16	FCSTSUMM	319	2053	320	146	4.8833	2021053
2021059	29	FCSTSUMM	337	358	337	931	5.5500	2021056
2021060	2	FCSTSUMM	343	1304	343	1934	6.5000	2021057
2021061	27	FCSTSUMM	349	1925	361	1828	287.0500	2021061

**Table 4-3: Summary of Cancelled Outages**

NANU	PRN	Type	Start day	Start Time	Stop day	Stop time	Ref
-	-	-	-	-	-	-	-

**Table 4-4: Summary of Forecast and Actual Unscheduled Outages**

NANU	PRN	Type	Start day	Start Time	Stop day	Stop time	Outage (hours)	Ref
2021058	22	UNUSUFN	336	1637	NA	NA	NA	E6

The constellation availability and continuity figures for the baseline constellation, and for all satellites, based on the NANU information are shown in the following table. Note that for continuity and availability, the baseline constellation is not affected if at least one of the satellites in an expanded slot is healthy, i.e. an outage on one of the satellites in an expanded slot does not affect the statistics for the baseline constellation.

**Table 4-5: Summary of NANU Statistics for Monitoring Period**

	Q4 2021
<b>Hrs</b>	2208
<b>total forecast downtime (all)</b>	708.00
<b>total forecast downtime (baseline)</b>	360.00
<b>total actual scheduled downtime (all)</b>	596.80
<b>total actual scheduled downtime (baseline)</b>	304.87
<b>Scheduled satellite outage events (all)</b>	5
<b>Scheduled satellite outage events (baseline)</b>	3
<b>Unscheduled satellite outage events (all)</b>	1
<b>Unscheduled satellite outage events (baseline)</b>	0
<b>Total actual unscheduled downtime (all)</b>	679.38
<b>Total actual unscheduled downtime (baseline)</b>	0.00
<b>Total actual downtime (all)</b>	1276.18
<b>Total actual downtime (baseline)</b>	304.87
<b>Availability (all)</b>	98.136
<b>Availability (baseline)</b>	99.425
<b>Continuity (baseline)</b>	100.000

Note also that a new satellite (which will take PRN11) was launched on 22<sup>nd</sup> June. It has not yet been set usable.



## 5. CONCLUSIONS

The following table summarises the measured performance against the specification.

**Table 5-1: Summary of Performance**

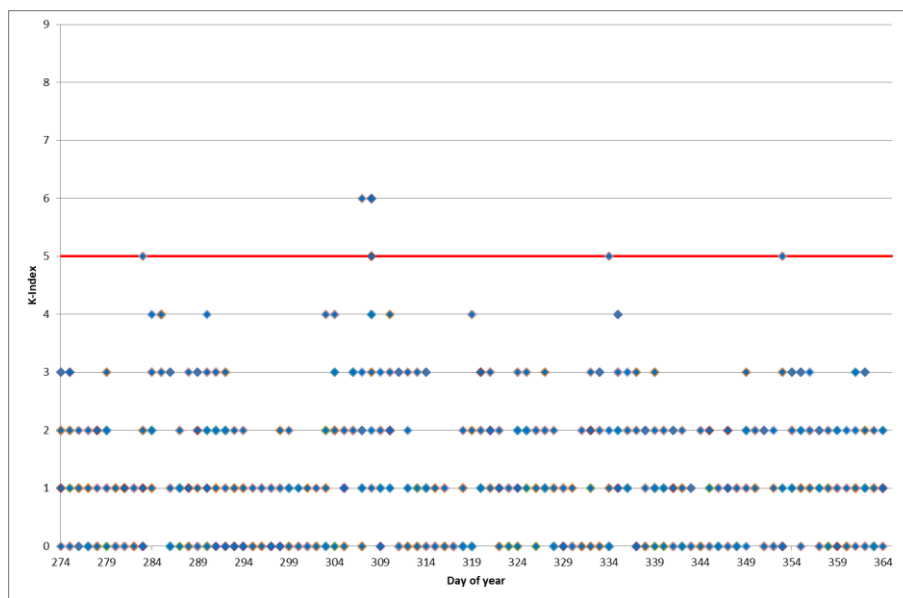
Criteria	Specifications	Measured Performance	Passed
SPS SIS Accuracy	The User Range Error (URE) $\leq 7$ m 95% for any satellite	Each SV < 7m	Yes.
	The User Range Error (URE) $\leq 2$ m 95% for all satellites	<3m	No
SPS SIS rms	$\leq 3.6$ m	All days <3.6m	Yes.
SPS SIS Integrity	The SIS Integrity $\leq 1 \times 10^{-5}$ Probability Over Any Hour (<0.7 events per quarter)	No SIS events	Yes
SPS SIS Continuity	$\geq 0.9998$ Probability Over Any Hour	100% (no unscheduled outages on baseline)  99.997% for rolling year	Yes, for both monitoring period and rolling year.
SPS SIS Availability	SPS SIS Per-Slot Availability <ul style="list-style-type: none"> <li><math>\geq 0.957</math></li> </ul> SPS SIS Constellation Availability <ul style="list-style-type: none"> <li><math>\geq 0.98</math> Probability that at least 21 Slots out of the 24 Slots will be healthy</li> <li><math>\geq 0.99999</math> Probability that at least 20 Slots out of the 24 Slots will be healthy</li> <li><math>\geq 0.95</math> Probability that the Constellation will have at least 24 Operational Satellites</li> </ul>	1) 99.9% per- Slot Availability  2) 100% Constellation Availability  3) 100% probability that the number of operational satellites is larger than 24.	Yes, for both monitoring period and rolling year.
PDOP Availability	<ul style="list-style-type: none"> <li><math>\geq 98\%</math> global PDOP of 6 or less</li> <li><math>\geq 88\%</math> worst site PDOP of 6 or less</li> </ul>	>99.8% availability on all days	Yes

Criteria	Specifications	Measured Performance	Passed
SPS Position Service Availability	<ul style="list-style-type: none"> <li>• <math>\geq 99\%</math> Horizontal Service Availability average location</li> <li>• <math>\geq 90\%</math> Horizontal Service Availability worst-case location</li> <li>• <math>\geq 99\%</math> Vertical Service Availability average location</li> <li>• <math>\geq 90\%</math> Vertical Service Availability worst-case location</li> </ul>	100% availability on all days	Yes
Positioning Accuracy	<ul style="list-style-type: none"> <li>• <math>\leq 8</math> meters 95% All-in-View Global Average Horizontal Error (SIS Only)</li> <li>• <math>\leq 15</math> meters 95% All-in-View worst site Horizontal Error (SIS Only)</li> <li>• <math>\leq 13</math> meters 95% All-in-View Global Average Vertical Error (SIS Only)</li> <li>• <math>\leq 33</math> meters 95% All-in-View worst site Vertical Error (SIS Only)</li> </ul>	1) $< 2.5$ metres 95% Horizontal Error at the site 2) $< 7.5$ metres 95% Vertical Error at the site	Yes

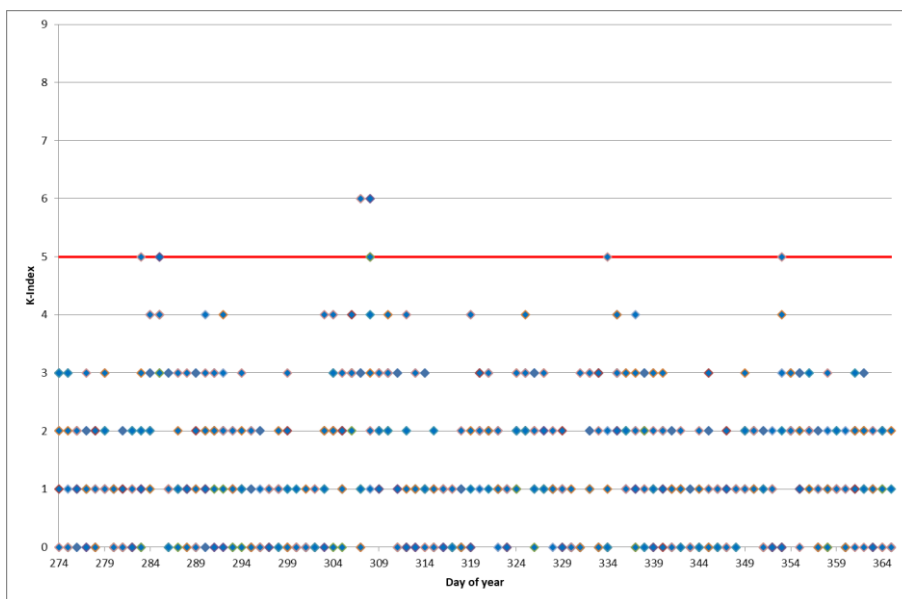
From the table it can be seen that the measured performance is within the required values for almost all requirements. The exception is the requirement of URE for all satellites combined being less than 2m.

## 6. APPENDIX A: GEOMAGNETIC DATA

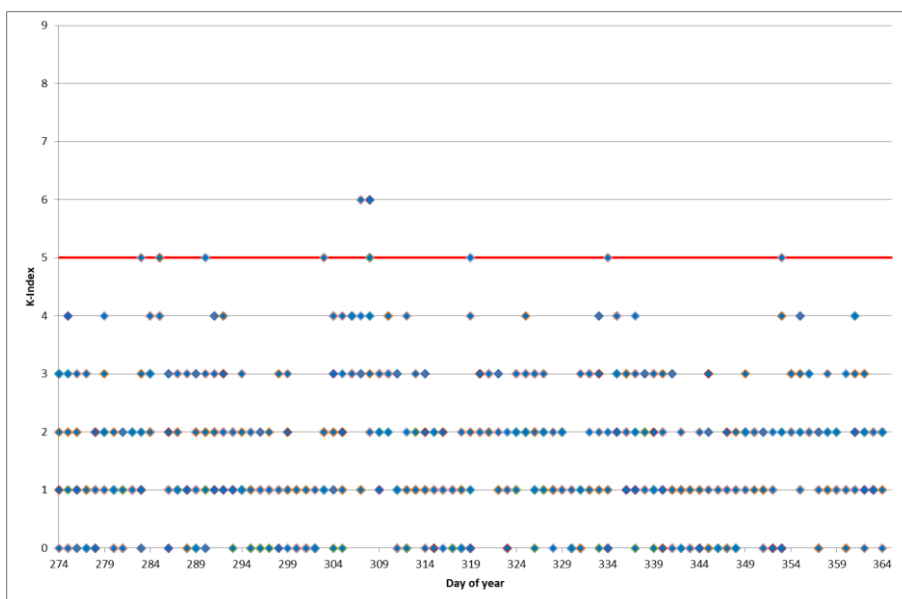
The solar activity during a particular period can be determined using the K index data provided by the British Geological Survey (BGS) in the UK. This data is available from [http://www.geomag.bgs.ac.uk/data\\_service/data/magnetic\\_indices/k\\_indices.html](http://www.geomag.bgs.ac.uk/data_service/data/magnetic_indices/k_indices.html). The K index at each observatory summarises the geomagnetic activity by assigning an index value (in the range 0 – 9) to each 3-hr time interval. The index values are determined from the maximum range in H or D with allowance made for the normal (undisturbed) diurnal variation. The conversion from range to index value is made using a quasi-logarithmic scale, with the scale values dependent on the geomagnetic latitude of the observatory. In general, the higher the K index the more active the Earth’s magnetic field. K-index values of 5 or higher indicate geomagnetic storm level activity and index values of 7 or higher indicate a severe geomagnetic storm. The geomagnetic activity is important to consider for GPS signals as geomagnetic storms may affect GPS performance, either by increasing the residual ionospheric delay errors in the position solution or by causing problems with tracking the satellite signals. The following figures show the K-index values at 3 sites in the UK during the monitoring period. The figures are reproduced with the permission of the British Geological Survey ©NERC. All rights reserved.



**Figure 6-1: K-Index Values at Lerwick during Reporting Period**



**Figure 6-2: K-Index Values at Eskdalemuir during Reporting Period**



**Figure 6-3: K-Index Values at Hartland during Reporting Period**

It can be seen that during the monitoring period there are only a few occasions where geomagnetic storm conditions (K index  $\geq 5$ ) are observed and generally it is a quiet period.

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